#### Alignment & Assembly Michael Schatz

Bioinformatics Lecture 3 Quantitative Biology 2011



#### **Exact Matching Review**

Where is GATTACA in the human genome? E=183,105



## Sequence Alignment Review





## Whole Genome Alignment with MUMmer

Slides Courtesy of Adam M. Phillippy <u>amp@umics.umd.edu</u>



• For two genomes, A and B, find a mapping from each position in A to its corresponding position in B



CCGGTAGGCTATTAAACGGGGGTGAGGAGCGTTGGCATAGCA

#### Not so fast...

 Genome A may have insertions, deletions, translocations, inversions, duplications or SNPs with respect to B (sometimes all of the above)



#### WGA visualization

- How can we visualize *whole* genome alignments?
- With an alignment dot plot T  $-N \times M$  matrix G• Let i = position in genome A• Let j = position in genome B• Fill cell (*i*,*j*) if  $A_i$  shows similarity to  $B_j$



 A perfect alignment between A and B would completely fill the positive diagonal



http://mummer.sourceforge.net/manual/AlignmentTypes.pdf

Α



## MUMmer

- <u>Maximal Unique Matcher (MUM)</u>
  - match
    - exact match of a minimum length
  - maximal
    - cannot be extended in either direction without a mismatch
  - unique
    - occurs only once in both sequences (MUM)
    - occurs only once in a single sequence (MAM)
    - occurs one or more times in either sequence (MEM)

#### **Fee Fi Fo Fum**, is it a MAM, MEM or MUM?

 MUM : maximal unique match

 MAM : maximal almost-unique match

 MEM : maximal exact match



## Seed and Extend

- How can we make MUMs **BIGGER?** 
  - I. Find MUMs
    - using a suffix tree
  - 2. Cluster MUMs
    - using size, gap and distance parameters
  - 3. Extend clusters
    - using modified Smith-Waterman algorithm

#### Seed and Extend visualization

#### FIND all MUMs CLUSTER consistent MUMs EXTEND alignments



#### WGA example with **nucmer**

- Yersina pestis CO92 vs. Yersina pestis KIM
  - High nucleotide similarity, 99.86%
    - Two strains of the same species
  - Extensive genome shuffling
    - Global alignment will not work
  - Highly repetitive
    - Many local alignments

#### WGA Alignment

#### nucmer -maxmatch CO92.fasta KIM.fasta

-maxmatch Find maximal exact matches (MEMs)

#### delta-filter -m out.delta > out.filter.m

-m Many-to-many mapping

#### show-coords -r out.delta.m > out.coords

-r Sort alignments by reference position

#### dnadiff out.delta.m

Construct catalog of sequence variations

#### mummerplot --large --layout out.delta.m

--large Large plot
--layout Nice layout for multi-fasta files
--x11 Default, draw using x11 (--postscript, --png)
\*requires gnuplot



#### References

#### Documentation

- http://mummer.sourceforge.net
  - » publication listing
- http://mummer.sourceforge.net/manual
  - » documentation
- http://mummer.sourceforge.net/examples
  - » walkthroughs
- Email
  - mummer-help@lists.sourceforge.net
  - amp@umiacs.umd.edu



# Bowtie: Ultrafast and memory efficient alignment of short DNA sequences to the human genome

Slides Courtesy of Ben Langmead (langmead@umiacs.umd.edu)

## Short Read Applications

• Genotyping: Identify Variations



• \*-seq: Classify & measure significant peaks



## Short Read Alignment

 Given a reference and a set of reads, report at least one "good" local alignment for each read if one exists

- Approximate answer to: where in genome did read originate?

- What is "good"? For now, we concentrate on:
  - Fewer mismatches is better
  - Failing to align a low-quality base is better than failing to align a high-quality base



# Indexing

- Genomes and reads are too large for direct approaches like dynamic programming
  - Genome indices can be big. For human:



- Large indices necessitate painful compromises
  - I. Require big-memory machine
  - 2. Use secondary storage

- 3. Build new index each run
- 4. Subindex and do multiple passes

#### **Burrows-Wheeler Transform**

Reversible permutation of the characters in a text



• BWT(T) is the index for T

implicitly encodes Suffix Array

A block sorting lossless data compression algorithm. Burrows M, Wheeler DJ (1994) Digital Equipment Corporation. Technical Report 124

#### **Burrows-Wheeler Transform**

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#### **Burrows-Wheeler Transform**

- Recreating T from BWT(T)
  - Start in the first row and apply LF repeatedly, accumulating predecessors along the way





BWT(Reference)





BWT(Reference)





BWT(Reference)



























# **BWT Short Read Mapping**

- Trim off very low quality bases & adapters from ends of sequences
- 2. Execute depth-first-search of the implicit suffix tree represented by the BWT
  - I. If we fail to reach the end, back-track and resume search
  - 2. BWT enables searching for good end-to-end matches entirely in RAM
    - I. 100s of times faster than competing approaches
- 3. Report the "best" n alignments
  - I. Best = fewest mismatches/edit distance, possibly weighted by QV
  - 2. Some reads will have millions of equally good mapping positions
  - 3. If reads are paired, try to find mapping that satisfies both

# Mapping Applications

- Mapping Algorithms
  - Bowtie: (BWT) Fastest, No indels => moderate sensitivity
  - BWA: (BWT) Fast, small indels => good sensitivity
  - Novoalign: (Hash Table) Slow, RAM intensive, big indels => high sensitivity
- Variation Detection
  - SNPs
    - SAMTools: Bayesian model incorporating depth, quality values, also indels
    - SOAPsnp: SAMTools + known SNPs, nucleotide specific errors, no indels
  - Structural Variations
    - Hydra: Very sensitive alignment, scan for discordant pairs
    - Large indels: Open Research Problem to assembly their sequence
  - Copy number changes
    - RDexplorer: Scan alignments for statistically significant coverage pileup
  - Microsatellite variations
    - See Mitch!

# Sequence Alignment Summary

- Distance metrics:
  - Hamming: How many substitutions?
  - Edit Distance: How many substitutions or indels?
  - Sequence Similarity: How similar (under this model of similarity)?
- Techniques
  - Seed-and-extend: Anchor the search for in-exact using exact only
  - Dynamic Programming: Find a global optimal as a function of its parts
  - BWT Search: implicit DFS of SA/ST
- Sequence Alignment Algorithms: Pick the right tool for the job
  - Smith-Waterman: DP Local sequence alignment
  - BLAST: Homology Searching
  - MUMmer: Whole genome alignment, short read mapping (with care)
  - Bowtie/BWA/Novoalign: short read mapping
### Break



- Nodes
  - People, Proteins, Genes, Neurons, Sequences, Numbers, ...
- Edges
  - A is connected to B
  - A is related to B
  - A regulates B
  - A precedes B
  - A interacts with B
  - A is related to B

- ...

# **Biological Networks**



Figure 5 Putative regulatory elements shared between groups of correlated and anticorrelated genes











# Graph Types



# Kevin Bacon and Bipartite Graphs

Q1: Find *any* path from Kevin Bacon to Jason Lee

Depth First Search: 6 hops

Bacon Distance: 3





# Kevin Bacon and Bipartite Graphs



### DFS

#### **DFS**(start, stop)

// initialize all nodes dist = -1start.dist = 0list.addEnd(start) while (!list.empty()) cur = list.end() if (cur == stop) print cur.dist; else foreach child in cur.children if (child.dist == -1) child.dist = cur.dist+llist.addEnd(child)

 $A,B,G,\underline{H}$ A,B,G,<u>M</u> A,B,<u>G</u> A,B,<u>L</u> A,B,<u>O</u> A,B,<u>N</u> A,B,<u>J</u> A,B,E,<u>F</u> A,B,E,<u>K</u> A,B,<u>E</u> A,<u>B</u> <u>A</u> <u>D</u> I E:7

<u>0</u> A,B,<u>C</u>

[How many nodes will it visit?]

[What's the running time?]

[What happens for disconnected components?]

### DFS

#### **DFS**(start, stop)

// initialize all nodes dist = -1
start.dist = 0
list.addEnd(start)
while (!list.empty())
 cur = list.end()
 if (cur == stop)
 print cur.dist;
 else
 foreach child in cur.children
 if (child.dist == -1)
 child.dist = cur.dist+1
 list.addEnd(child)

**F:7** 

<u>0</u> A,B,<u>C</u> A,B,G,<u>H</u> A,B,G,<u>M</u> A,B,<u>G</u> A,B,<u>L</u> A,B,<u>O</u> A,B,<u>N</u> A,B,<u>J</u> A,B,E,<u>F</u> A,B,E,K A,B,<u>E</u> А,<u>В</u> <u>A</u> <u>D</u>

0

# BFS

**BFS**(start, stop) // initialize all nodes dist = -1start.dist = 0list.addEnd(start) while (!list.empty()) cur = list.begin() if (cur == stop) print cur.dist; else foreach child in cur children if (child.dist == -1) child.dist = cur.dist+1list.addEnd(child) D:2 **F:**2

G:2

H:2

A,B,C B,C,D,E <u>C</u>,D,E,F,L D,E,F,L,G,H <u>E</u>,F,L,G,H,I <u>F</u>,L,G,H,I,J L,G,H,I,J,K <u>G</u>,H,I,J,K,O <u>H</u>,I,J,K,O I,J,K,O,M J,K,O,M <u>K</u>,O,M,N <u>O</u>,M,N <u>M</u>,N Ν

### **BFS** and **TSP**

- BFS computes the shortest path between a pair of nodes in  $O(|E|) = O(|N|^2)$
- What if we wanted to compute the shortest route visiting every node once?
  - Traveling Salesman Problem



# Greedy Search

#### **Greedy Search**

cur=graph.smallestEdge()
while (!done)
next=cur.getNextClosest()



Greedy: ABDCA = 1+1+1+50=53Optimal: ACBDA = 1+19+1+21=42

Greedy finds the global optimum only when

- I. Greedy Choice: Local is correct without reconsideration
- 2. Optimal Substructure: Problem can be split into subproblems

Optimal Greedy: Making change with the fewest number of coins

# **TSP Hardness**

- No known way to partition the problem
  - Knowing optimal tour through n cities doesn't seem to help much for n+I cities

[How many possible tours for n cities?]

- Extensive searching is the only known provably correct algorithm
  - Brute Force:
    - ~20 cities max
    - 20! =  $2.4 \times 10^{18}$





# Branch-and-Bound

- Abort on suboptimal solutions as soon as possible
  - ADBECA = 1+2+2+2+3 = 10
  - ABDE = 4+2+30 > 10
  - -ADE = |+30 > |0|
  - AED = I + 30 > 10

— …

- Performance Heuristic
  - Always gives the optimal answer
  - Doesn't always help performance, but often does
  - Current TSP record holder:
    - 85,900 cities
    - 85900! =  $10^{386526}$



[When not?]

# **TSP and NP-complete**

- TSP is one of many extremely hard problems of the class NP-complete
  - Extensive searching is the only way to find an exact solution
  - Often have to settle for approx. solution



- WARNING: Many optimization problems are in this class
  - Find a tour the visits every node once
  - Find the smallest set of vertices covering all the edges
  - Find the largest clique in the graph
  - Find a set of items with maximal value but limited weight
  - Maximizing the number of tetris pieces played
  - ...
  - http://en.wikipedia.org/wiki/List\_of\_NP-complete\_problems

## Shortest Common Superstring

Given:  $S = \{s_1, ..., s_n\}$ 

Problem: Find minimal length superstring of S

 $s_{1}, s_{2}, s_{3} = CACCCGGGTGCCACC \quad 15$   $s_{1} CACCC \qquad s_{1}, s_{3}, s_{2} = CACCCACCGGGTGC14$   $s_{2} CCGGGTGC \qquad s_{2}, s_{1}, s_{3} = CCGGGTGCACCCACC \quad 15$   $s_{3} CCACC \qquad s_{2}, s_{3}, s_{1} = CCGGGTGCCACCC \quad 13$   $s_{3}, s_{1}, s_{2} = CCACCCGGGTGC \quad 12$   $s_{3}, s_{2}, s_{3} = CCACCGGGTGCACCC \quad 15$ 

NP-Complete by reduction from VERTEX-COVER and later DIRECTED-HAMILTONIAN-PATH

# Paths through graphs and assembly

- Hamiltonian circuit: visit each node (read) exactly once, returning to the start
  - If we could do this fast, we could exactly assemble genomes as the shortest common superstring



# Assembling a Genome



2. Construct assembly graph from overlapping reads

...AGCCTAGACCTACAGGATGCGCGACACGT GGATGCGCGACACGTCGCATATCCGGT...

3. Simplify assembly graph



4. Detangle graph with long reads, mates, and other links



# Illumina Sequencing by Synthesis



http://www.illumina.com/documents/products/techspotlights/techspotlight\_sequencing.pdf

# Paired-end and Mate-pairs

#### Paired-end sequencing

- Read one end of the molecule, flip, and read the other end
- Generate pair of reads separated by up to 500bp with inward orientation

#### Mate-pair sequencing

- Circularize long molecules (1-10kbp), shear into fragments, & sequence
- Mate failures create short paired-end reads

10kbp



### Typical contig coverage



Imagine raindrops on a sidewalk

### Genome Coverage Distribution



This is the mathematically model => reality may be much worse

# **Coverage and Read Length**

#### Idealized Lander-Waterman model

- Reads start at perfectly random positions
- Poisson distribution in coverage
  - Contigs end when there are no overlapping reads
- Contig length is a function of coverage and read length
  - Effective coverage reduced by o/l
  - Short reads require much higher coverage to reach same expected contig length





Assembly of Large Genomes using Second Generation Sequencing Schatz MC, Delcher AL, Salzberg SL (2010) *Genome Research*. 20:1165-1173.

# Two Paradigms for Assembly



Short read assemblers

- Repeats depends on word length
- Read coherency, placements lost
- Robust to high coverage



Long read assemblers

- Repeats depends on read length
- Read coherency, placements kept
- Tangled by high coverage

Assembly of Large Genomes using Second Generation Sequencing Schatz MC, Delcher AL, Salzberg SL (2010) *Genome Research*. 20:1165-1173.

### Initial Contigs

- After simplification and correction, compress graph down to its non-branching initial contigs
  - Aka "unitigs", "unipaths"





# **Repeats and Read Length**



- Explore the relationship between read length and contig N50 size
  - Idealized assembly of read lengths: 25, 35, 50, 100, 250, 500, 1000
  - Contig/Read length relationship depends on specific repeat composition

Assembly Complexity of Prokaryotic Genomes using Short Reads. Kingsford C, Schatz MC, Pop M (2010) *BMC Bioinformatics*. 11:21.

# Repetitive regions

• Over 50% of the human genome is repetitive

Repeat Type	Definition / Example	Prevalence
Low-complexity DNA / Microsatellites	$(b_1b_2b_k)^N$ where $I \le k \le 6$ CACACACACACACACACACACA	2%
SINEs (Short Interspersed Nuclear Elements)	<i>Alu</i> sequence (~280 bp) Mariner elements (~80 bp)	13%
LINEs (Long Interspersed Nuclear Elements)	~500 – 5,000 bp	21%
LTR (long terminal repeat) retrotransposons	Ту I -copia, Ту3-gypsy, Pao-BEL (~100 – 5,000 bp)	8%
Other DNA transposons		3%
Gene families & segmental duplications		4%



- If *n* reads are a uniform random sample of the genome of length *G*, we expect  $k=n\Delta/G$  reads to start in a region of length  $\Delta$ .
  - If we see many more reads than k (if the arrival rate is > A), it is likely to be a collapsed repeat
  - Requires an accurate genome size estimate

$$\Pr(X - copy) = \binom{n}{k} \left(\frac{X\Delta}{G}\right)^{k} \left(\frac{G - X\Delta}{G}\right)^{n-k} \qquad A(\Delta, k) = \ln\left(\frac{\Pr(1 - copy)}{\Pr(2 - copy)}\right) = \ln\left(\frac{\frac{(\Delta n/G)^{k}}{k!}e^{\frac{-\Delta n}{G}}}{\frac{(2\Delta n/G)^{k}}{k!}e^{\frac{-2\Delta n}{G}}}\right) = \frac{n\Delta}{G} - k\ln 2$$

# Scaffolding

- Initial contigs (aka unipaths, unitigs) terminate at
  - Coverage gaps: especially extreme GC regions
  - Conflicts: sequencing errors, repeat boundaries
- Iteratively resolve longest, 'most unique' contigs
  - Both overlap graph and de Bruijn assemblers initially collapse repeats into single copies
  - Uniqueness measured by a statistical test on coverage



### N50 size

#### Def: 50% of the genome is in contigs larger than N50



```
N50 size = 30 \text{ kbp}
```

```
(300k+100k+45k+45k+30k = 520k \ge 500kbp)
```

Note:

N50 values are only meaningful to compare when base genome size is the same in all cases

### Assembly Algorithms





- Attempt to answer the question:
   "What makes a good assembly?"
- Organizers provided simulated sequence data
  - Simulated 100 base pair Illumina reads from simulated diploid organism
- 41 submissions from 17 groups
- Results demonstrate trade-offs assemblers must make

# **Assembly Results**



No assembler was perfect!
 – See tomorrow's in house for details

# Summary



Graphs are ubiquitous in the world

- Pairwise searching is easy, finding features is hard

Assembly quality depends on

- I. Coverage: low coverage is mathematically hopeless
- 2. Repeat composition: high repeat content is challenging
- 3. Read length: longer reads help resolve repeats
- 4. Error rate: errors reduce coverage, obscure true overlaps

Assembly is a hierarchical, starting from individual reads, build high confidence contigs/unitigs, incorporate the mates to build scaffolds

 Extensive error correction is the key to getting the best assembly possible from a given data set

### Supplemental

## **BWT Exact Matching**

 LFc(r, c) does the same thing as LF(r) but it ignores r's actual final character and "pretends" it's c:



# **BWT Exact Matching**

 Start with a range, (top, bot) encompassing all rows and repeatedly apply LFc:
 top = LFc(top, qc); bot = LFc(bot, qc)

**qc** = the next character to the left in the query



Ferragina P, Manzini G: Opportunistic data structures with applications. FOCS. IEEE Computer Society; 2000.

### **BWT Exact Matching**



 If range becomes empty (top = bot) the query suffix (and therefore the query as a whole) does not occur